

# END TERM EXAMINATION

SECOND SEMESTER [BCA] MAY-JUNE 2017

Paper Code: BCA-102

Subject: Mathematics-II

Time: 3 Hours

Maximum Marks: 75

Note: Attempt any five questions including Q.no.1 which is compulsory. Select one question from each Unit.

- Q1 (a) Let  $A = \{1, 2, 3\}$  and  $B = \{a, b, c\}$ . Let  $R = \{(1, b)(1, c)(3, b)\}$ . Find the domain and range of the relation. Determine  $R^{-1}$ . (3)
- (b) Let  $D$  denote the set of all positive divisors of the positive integer  $n$ . Determine  $D_{16}$ , and represent it by Hasse Diagram. (2)
- (c) Define isomorphic and Hamilton Graphs with example. (3)
- (d) Let  $f, g$ , be functions from  $N$  to  $N$  (set of natural numbers) for  $N \in N$  such that  $f(n) = n + 1, g(n) = 2n$ . Find  $f \circ g$  and  $g \circ f$ . (3)
- (e) Define Tautology and contradictions. (2)
- (f) Show that the relation of parallel lines in the set of lines on a plane is an equivalence relation. (2)
- (g) Choose any two statements  $p$  and  $q$  as you like. Draw the truth table for  $p \wedge q$ , and  $p \vee q$ . (2)
- (h) Consider the graph  $G (V, E)$  where  $v$  consists of Four vertices  $A, B, C, D$  and  $E$  of five edges where  $e_1 = \{A, B\}, e_2 = \{B, C\}, e_3 = \{C, D\}, e_4 = \{A, C\}$  and  $e_5 = \{B, D\}$ , represent this undirected graph diagrammatically. Determine the degree of each vertex. (3)
- (i) Let  $f$  be a mapping from  $R$  to  $R$  such that  $f(x) = 2x + 3$ . Show that  $f$  is invertible and find its inverse. (3)
- (j) If  $n(A) = 40, n(B) = 30, n(A \cap B) = 20$ . Then find  $n(A \cup B)$ . (2)

### Unit-I

- Q2 (a) Let  $A = \{1, 2, 5, 6\}, B = \{2, 5, 7\}, C = \{1, 3, 5, 7, 9\}$ . Verify  $(A \times B) \cap \{A \times C\} = A \times \{B \times C\}$ . (6)
- (b) Let  $N = \{1, 2, 3, \dots\}$ , denote the set of all positive integers and  $A = \{x : x \in N, 3 < x < 12\}, B = \{x : x \in N, x \text{ is even}, x < 15\}$ . Find  $A \cap B, A \cup B, A^c$  and  $B^c$ . (6.5)
- Q3 (a) If  $R$  is an equivalence relation in a set  $A$ . Then prove that  $R^{-1}$  is also equivalence relation. (6)
- (b) For the sets  $A, B, C$  prove the following results.  
 (i)  $A - (B \cap C) = (A - B) \cup (A - C)$ , (ii)  $A \times (B \cup C) = (A \times B) \cup (A \times C)$ . (6.5)

### Unit-II

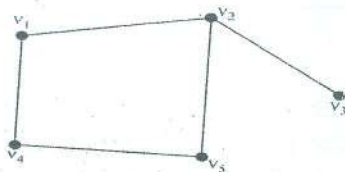
- Q4 (a) In a lattice  $(L, \leq)$ , prove that  
 (i)  $a \wedge (b \vee c) \geq (a \wedge b) \vee (a \wedge c)$ . (ii)  $a \vee (b \wedge c) \leq (a \vee b) \wedge (a \vee c)$ . (6)
- (b) Define Bounded lattice and prove that every lattice  $L$  is bounded. (6.5)
- Q5 (a) Define complemented lattice, also find the complement (if exists) of all elements of  $(D_{30}, I)$ . (6.5)
- (b) Let  $A = \{1, 2, 3, 4, 6, 8, 9, 12, 18, 24\}$  be equipped with relation  $x$  divides  $y$ . Draw the Hasse diagram. (6)

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**Unit-III**

- Q6 (a) Let  $G$  be an undirected graph with  $m$  vertices, say  $v_1, v_2, v_3, \dots, v_m$ . Define the adjacent matrix  $A$  of  $G$ . Consider the undirected graph  $G$  with 5 vertices  $v_1, v_2, v_3, v_4, v_5$  shown in the following diagram. Find the adjacent matrix of this graph. (6.5)

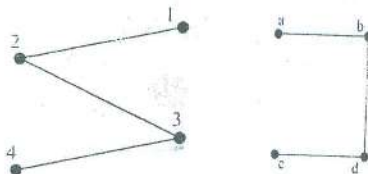


- (b) Draw the directed graph for the following incident matrix. Also find the degree of all vertex.

$$\begin{matrix} & e_1 & e_2 & e_3 & e_4 & e_5 & e_6 & e_7 & e_8 \\
 v_1 & \begin{bmatrix} -1 & 0 & 0 & 0 & -1 & -1 & 1 & 0 \end{bmatrix} \\
 v_2 & \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \\
 v_3 & \begin{bmatrix} 0 & -1 & -1 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \\
 v_4 & \begin{bmatrix} 0 & 0 & 1 & 1 & 0 & 0 & -1 & 0 \end{bmatrix} \\
 v_5 & \begin{bmatrix} 0 & 0 & 0 & -1 & 1 & 0 & 0 & -1 \end{bmatrix}
 \end{matrix}$$

(6)

- Q7 (a) Show that the two graphs shown in the figure are Isomorphic. (6.5)



- (b) Prove that the union of two graphs  $G_1$  and  $G_2$  will be a graph such that.

$$V(G_1 \cup G_2) = V(G_1) \cup V(G_2) \text{ and } E(G_1 \cup G_2) = E(G_1) \cup E(G_2). \quad (6)$$

**Unit-IV**

- Q8 (a) By means of truth tables, justify that the conditional statement "If  $p$  then  $q$ " is logically equivalent to the statement "Not  $p$  or  $q$ ". (6.5)  
 (b) Define a proposition. Let  $p$  and  $q$  be propositions and  $p \rightarrow q$  denote compound proposition, "if  $p$  then  $q$ ". Draw the truth table for the compound proposition  $p \rightarrow q$ . Let  $p$ : you try, and  $q$ : you will succeed. Justify the truth table for  $p \rightarrow q$ . (6)
- Q9 (a) Verify De-morgan's laws for propositions. And also prove that. (6.5)  

$$P \wedge (q \vee r) = (p \wedge q) \vee (p \wedge r).$$
  
 (b) Consider the following: (6)  
 $P$ : Today is Tuesday,  $Q$ : It is raining,  $R$ : It is cold.

Write in simple sentence the meaning of the following:

- (i)  $\sim q \rightarrow (r \wedge q)$   
 (ii)  $(p \vee q) \leftrightarrow r$

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